

Thermal Fluids I

January 17, 2007

Handout is on-line at: evan.lemley.org

- HW#2 – due Friday Jan. 26 by 5:00 p.m.
- 3.16, 3.20, 3.34, 3.38, 3.47, 3.54, 3.57
- Lecture on calculating work done by ideal gas
- Work done by system on boundary is:

$$W = \int_{V_1}^{V_2} p \, dV$$

- This form is used for expansion and contraction of gases

• Ideal Gases

• **Ideal (Perfect) Gas Law**

- $pV = n\bar{R}T$

- $\bar{R} = 8.314 \frac{kJ}{kgmol-K}$

- The gas constant for a particular gas (air in this example) may be found as

- $R_{air} = \frac{\bar{R}}{M_{air}} = \frac{8.314 \frac{kJ}{kgmol-K}}{28.97 \frac{kg}{kgmol}} = 0.287 \frac{kJ}{kg-K}$

- Rewrite the Ideal Gas Law in terms of mass and the gas constant for air in this example as

- $pV = m_{air} R_{air} T$

• **Isotropic (Constant Temp) Process**

- For a constant temperature process in a closed system (i.e. mass is constant) – $pV = mRT = C$. Where C is a constant. Note C can be written as p_1V_1 or as p_2V_2 .

- $W = \int_{V_1}^{V_2} \frac{C}{V} dV = C \ln\left(\frac{V_2}{V_1}\right) = p_1 V_1 \ln\left(\frac{V_2}{V_1}\right)$

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• **Polytropic process - $pV^n = C$ where C is a constant.**

- these occur in ideal gases for various processes and the value of n changes depending on the type of process (e.g. $n = 1$ is a isotropic process).

- Note that $p_1 V_1^n = C \rightarrow p_1 V_1 = \frac{C V_1}{V_1^n} = C V_1^{1-n}$ This also holds for $p_2 V_2$.

- $W = \int_{V_1}^{V_2} \frac{C}{V^n} dV = \frac{C}{1-n} (V_2^{1-n} - V_1^{1-n}) = \frac{p_2 V_2 - p_1 V_1}{1-n}$